## City University of Hong Kong Course Syllabus

# offered by College/School/Department of <u>Mathematics</u> with effect from Semester <u>B</u> <u>20 19 / 20</u>

Part I Course Over	view
Course Title:	Linear Algebra with Applications
Course Code:	MA1503
Course Duration:	1 Semester
Credit Units:	4
Level:	_B1
Proposed Area:	☐ Arts and Humanities ☐ Study of Societies, Social and Business Organisations ☐ Science and Tachnology
(for GE courses only)  Medium of	English
Instruction:  Medium of Assessment:	English
Prerequisites: (Course Code and Title)	(i) HKDSE Mathematics Compulsory Part, or (ii) HKDSE Mathematics Compulsory Part and Extended Part Module 1, or (iii) HKDSE Mathematics Compulsory Part and Extended Part Module 2 (Levels 1 – 3); or equivalent
Precursors: (Course Code and Title)	Nil
<b>Equivalent Courses</b> : (Course Code and Title)	Nil
Exclusive Courses: (Course Code and Title)	MA1200 Calculus and Basic Linear Algebra I MA1201 Calculus and Basic Linear Algebra II MA1300 Enhanced Calculus and Linear Algebra I MA1301 Enhanced Calculus and Linear Algebra II

1

#### Part II **Course Details**

#### 1. **Abstract**

(A 150-word description about the course)

This course introduces the theory and applications of linear algebra and matrices. It will help students to develop a logical and systematic understanding of the core material of linear algebra, and apply linear algebra methods to create and formulate mathematical models in science and related fields.

#### 2. **Course Intended Learning Outcomes (CILOs)**

(CILOs state what the student is expected to be able to do at the end of the course according to a given standard of performance.)

No.	CILOs#	Weighting* (if applicable)	curric learnii (pleas	very-enrulum reng outcome tick we bropriat	lated omes where
1.	Explain clearly concepts from vector and matrix algebra	10%	√ √	712	715
2.	Perform basic operations and solve equations involving complex numbers	10%	√		
3.	Evaluate mathematical quantities of matrices and vector spaces by Gaussian elimination, diagonalization, and other algorithms	25%		√	
4.	Develop a logical and systematic understanding of the structure of the Euclidean vector spaces, and demonstrate this in some practical problems	15%	V	√	
5.	Apply linear algebra methods to various subjects, and create and formulate mathematical models to a range of problems in science and engineering involving linear structures	15%	V	V	√
6.	The combination of CILOs 1 – 5	25%	<b>V</b>	<b>√</b>	<b>√</b>
* If we	eighting is assigned to CILOs, they should add up to 100%.	100%			

<sup>\*</sup> If weighting is assigned to CILOs, they should add up to 100%.

Develop an attitude of discovery/innovation/creativity, as demonstrated by students possessing a strong sense of curiosity, asking questions actively, challenging assumptions or engaging in inquiry together with teachers.

#### *A2*: Ability

Develop the ability/skill needed to discover/innovate/create, as demonstrated by students possessing critical thinking skills to assess ideas, acquiring research skills, synthesizing knowledge across disciplines or applying academic knowledge to self-life problems.

### Accomplishments

Demonstrate accomplishment of discovery/innovation/creativity through producing /constructing creative works/new artefacts, effective solutions to real-life problems or new processes.

#### 3. **Teaching and Learning Activities (TLAs)**

(TLAs designed to facilitate students' achievement of the CILOs.)

Indicative of likely activities and tasks students will undertake to learn in this course. Final details will be provided to students in their first week of attendance in this course.

<sup>#</sup> Please specify the alignment of CILOs to the Gateway Education Programme Intended Learning outcomes (PILOs) in Section A of Annex.

TEL A	Delet Description			CILO		Hours/week (if		
TLA	Brief Description	1	2	3	4	5	6	applicable)
Lectures	Learning through <b>teaching</b> is primarily based on lectures.	<b>✓</b>	<b>✓</b>	<b>✓</b>	<b>✓</b>	<b>✓</b>	✓	39 hours in total
	Learning through <b>tutorials</b> is		<b>√</b>					4 hours
	primarily based on interactive			✓	<b>√</b>			4 hours
Tutorials	problem solving allowing instant				· ·			2 hours
	feedback.	✓				✓	✓	2 hours
	Learning through take-home							
	assignments helps students							
	understand basic mathematical							
Assignments	concepts and fundamental theory	<b>✓</b>	<b>✓</b>	✓	✓	<b>√</b>	<b>✓</b>	after-class
	of linear algebra, and develop the							
	ability of proving mathematical							
	statements rigorously.							
	Learning through <b>online</b>							
	examples for applications helps							
Online	students create and formulate				<b>√</b>		<b>√</b>	after-class
applications	simple mathematical models and				ľ	•	ľ	arter-class
	apply to some problems in science							
	and engineering.							
N. 4. 17. 1	Learning activities in Math Help							
Math Help Centre	Centre provides students extra	✓	✓	✓	✓	✓	✓	after-class
	help.							

### 4. Assessment Tasks/Activities (ATs)

(ATs are designed to assess how well the students achieve the CILOs.)

30% Coursework

70% Examination (Duration: 3 hours, at the end of the semester)

For a student to pass the course, at least 30% of the maximum mark for the examination must be obtained.

Assessment		CILO No.					Waighting*	Remarks	
Tasks/Activities	1	2	3	4	5	6	Weighting*	Remarks	
Continuous Assessment:30%									
Quizzes/Test(s)	<b>√</b>	<b>√</b>	<b>√</b>	<b>√</b>	<b>√</b>	<b>√</b>	25%	Questions are designed for the first part of the course to see how well the students have learned the basic concepts and fundamental theory of linear algebra, and have developed the ability of proving mathematical statements rigorously.	

Assessment	CILO No.				Weighting*	Remarks		
Tasks/Activities	1	2	3	4	5	6	weighting.	Kemarks
Formative take-home assignments	<b>✓</b>	<b>✓</b>	<b>✓</b>	<b>✓</b>	<b>✓</b>	✓	5%	The assignments provide students chances to demonstrate their achievements on linear algebra learned in this course.
Examination: (duration: 3 hrs)	✓	<b>√</b>	<b>√</b>	<b>√</b>	<b>√</b>	✓	70%	Examination questions are designed to see how far students have achieved their intended learning outcomes. Questions will primarily be skills and understanding based to assess the student's versatility in linear algebra.
* The weightings should add up to 100%.						100%		

### 5. Assessment Rubrics

(Grading of student achievements is based on student performance in assessment tasks/activities with the following rubrics.)

Assessment Task	Criterion	Excellent (A+, A, A-)	Good (B+, B, B-)	Fair (C+, C, C-)	Marginal (D)	Failure (F)
1. Test	<ul> <li>1.1 UNDERSTANDING of the basic concepts and theory of linear algebra</li> <li>1.2 ABILITY to PROVE mathematical statements rigorously</li> </ul>	High	Significant	Moderate	Basic	Not even reaching marginal levels
2. Hand-in Assignments	2.1 DEMONSTRATION of the understanding of the basic materials	High	Significant	Moderate	Basic	Not even reaching marginal levels
3. Formative take-home assignments	3.1 DEMONSTRATION of the understanding of the basic materials	High	Significant	Moderate	Basic	Not even reaching marginal levels
4. Examination	4.1 DEMONSTRATION of skills and versatility in linear algebra	High	Significant	Moderate	Basic	Not even reaching marginal levels

### Part III Other Information (more details can be provided separately in the teaching plan)

### 1. Keyword Syllabus

(An indication of the key topics of the course.)

- A) Vectors in R<sup>2</sup> and R<sup>3</sup>; Scalar (dot) products, cross products, triple scalar products; Linear (in)dependence
- B) Matrices; Determinants, cofactor expansion; Systems of linear equations, Gaussian elimination, Cramer's rule; Matrix inverses, Gauss-Jordan elimination method
- C) Eigenvalues and Eigenvectors. Similarity and Diagonalization
- D) Vector spaces, subspace, rank; Fundamental theorems of linear algebra
- E) Linear Transformations; Quadratic Form and Positive Definite Matrices; Orthogonal and Unitary Transformation

### 2. Reading List

### 2.1 Compulsory Readings

(Compulsory readings can include books, book chapters, or journal/magazine articles. There are also collections of e-books, e-journals available from the CityU Library.)

1.	(Lay 2012) Linear Algebra and Its Applications, by David, C. Lay, Pearson 2012.
2.	(Meyer 2000) Matrix Analysis and Applied Linear Algebra, by C. D. Meyer, SIAM 2000.

### 2.2 Additional Readings

(Additional references for students to learn to expand their knowledge about the subject.)

1.	(Nicholson, 2018) Linear Algebra with Applications, by W. Keith Nicholson, Open Edition, 2018
2	(Trefethen and Bau 1997) Numerical Linear Algebra, by L. N. Trefethen and D. Bau III, SIAM 1997. (nice introduction to numerical linear algebra, suitable for beginners)
3.	(Axler 2004) Linear Algebra Done Right (2nd edition), by S. Axler, Springer 2004. (advanced text suitable for math majors and graduates, very well written and unique in its determinant-free approach)