## City University of Hong Kong Course Syllabus

# offered by Department of Computer Science with effect from Semester A 2019/20

Part I Course Over	view
Course Title:	Topics in Optimization and its Applications in Computer Science
Course Code:	CS6491
Course Duration:	One semester
Credit Units:	3 credits
Level:	_P6
Medium of Instruction:	English
Medium of Assessment:	English
	CS4335 Design and Analysis of Algorithms AND
Prerequisites: (Course Code and Title)	(MA2170 Linear Algebra & Multi-variable Calculus <u>or</u> MA2176 Basic Calculus and Linear Algebra)
<b>Precursors</b> : (Course Code and Title)	Nil
<b>Equivalent Courses</b> : (Course Code and Title)	Nil
Exclusive Courses: (Course Code and Title)	Nil

#### Part II Course Details

#### 1. Abstract

The goal of this course is to expose students to modern and fundamental developments of optimization theory, algorithms and applications in computer science. The course focus is on various topics including the conceptual and algorithmic sides of convex optimization as well as dynamic programming. We will cover cone programming including linear, quadratic and semidefinite programming, geometric programming and dynamic programming whose rich expressive power makes it suitable for a wide spectrum of important optimization problems arising in mathematics and computer science. On the algorithmic side, the course covers efficient methods including optimization decomposition, convex relaxation and iterative methods, e.g., proximal algorithms, to address large-scale problems and non-convex problems. Emphasis will also be placed on the software aspect of convex optimization and dynamic programming. A variety of applications in computer science will be selectively drawn from combinatorial graph problems, Internet and wireless networks, online social networks, machine learning, statistical inference, compressed sensing and artificial intelligence.

### 2. Course Intended Learning Outcomes (CILOs)

(CILOs state what the student is expected to be able to do at the end of the course according to a given standard of performance.)

At the end of the course, students are expected to be able to:

No.	CILOs	Weighting Discovery-enriche				
		(if	curricu	lum rel	ated	
		applicable)	learnin	g outco	mes	
			(please	tick	where	
			appropriate)			
			<i>A1</i>	A2	A3	
1.	analyze and explain topics in theory of optimization;		✓	✓		
2.	apply algorithms and techniques learned to solve practical problems;		✓	✓	✓	
	problems,					
3.	conduct scientific investigation in these areas.		✓	✓	<b>√</b>	
•		100%				

#### A1: Attitude

Develop an attitude of discovery/innovation/creativity, as demonstrated by students possessing a strong sense of curiosity, asking questions actively, challenging assumptions or engaging in inquiry together with teachers.

#### A2: Ability

Develop the ability/skill needed to discover/innovate/create, as demonstrated by students possessing critical thinking skills to assess ideas, acquiring research skills, synthesizing knowledge across disciplines or applying academic knowledge to self-life problems.

#### A3: Accomplishments

Demonstrate accomplishment of discovery/innovation/creativity through producing /constructing creative works/new artefacts, effective solutions to real-life problems or new processes.

## 3. Teaching and Learning Activities (TLAs)

(TLAs designed to facilitate students' achievement of the CILOs.)

Teaching pattern:

Suggested lecture/tutorial/laboratory mix: 2 hrs. lecture; 1 hr. tutorial

TLA	LA Brief Description			No.	Hours/week (if applicable)
		1	2	3	
Lecture	Lecture to teach basic concepts in optimization theory, teach problem-solving skills to analyse optimization problems and design algorithms to compute the solution, and to guide students on applying optimization theory and algorithms to a variety of applications in computer science.	<b>√</b>	<b>V</b>	<b>√</b>	
Tutorials	Tutorials for students to learn basic concepts in optimization theory, problem-solving skills to analyse optimization problems, design algorithms to compute the solution, and to conduct scientific investigations of applying optimization theory to computer science and other practical applications.	<b>√</b>	<b>√</b>	<b>√</b>	
Homework Assignment	Homework assignment which includes analytical and numerical tasks covering basic concepts in optimization theory as well as problem-solving skills to analyse optimization problems and design algorithms as part of scientific investigation for practical applications of optimization theory.	<b>√</b>	<b>V</b>	<b>√</b>	
Midterm Examination	Midterm exam which includes analytical tasks covering basic concepts in optimization theory as well as problem-solving skills to analyse optimization problems and design algorithms to compute the solution.	<b>✓</b>	<b>✓</b>		

## 4. Assessment Tasks/Activities (ATs)

(ATs are designed to assess how well the students achieve the CILOs.)

Assessment Tasks/Activities	CILO No.		Weighting	Remarks				
	1	2	3					
Continuous Assessment: 40%								
Homework Assignment	✓	✓	✓	20%	2 weeks to complete			
Midterm Examination	✓	✓		20%	2 hours closed book			
Final Examination Assessment <sup>*</sup> : <u>60</u> % (duration: 2 hours)								
Final Examination	✓	✓		60%	Closed book			
				100%				

<sup>&</sup>lt;sup>^</sup> For a student to pass the course, at least 30% of the maximum mark for the examination must be obtained.

## 5. Assessment Rubrics

(Grading of student achievements is based on student performance in assessment tasks/activities with the following rubrics.)

Assessment Task	Criterion	Excellent	Good	Fair	Marginal	Failure
		(A+, A, A-)	(B+, B, B-)	(C+, C, C-)	(D)	(F)
Homework	Able to solve analytical	Excellent if the	Good if final	Fair if a weak	Marginal if feeble	Not even reaching
assignment	and numerical tasks	assignment has	answer is correct	attempt is made	attempt is made in	marginal levels.
	related to optimization	completely correct	with partially	in assignment and	assignment and no	
	theory and algorithms	solution with correct	correct workings	computer	computer	
	with a number of	workings and a	and a working	programming for	programming for	
	computer programming	working computer	computer	numerical tasks in	numerical tasks in	
	tasks satisfying CILOs 1	program for numerical	program for	the scientific	the scientific	
	2, and 3.	tasks in the scientific	numerical tasks in	investigation to	investigation to	
		investigation to apply	the scientific	apply	apply optimization	
		optimization theory.	investigation to	optimization	theory.	
			apply	theory.		
			optimization			
			theory.			
Midterm	Able to solve analytical	Excellent if the	Good if final	Fair if a weak	Marginal if feeble	Not even reaching
Examination	tasks related to	midterm exam has	answer is correct	attempt is made	attempt is made in	marginal levels.
	optimization theory and	completely correct	with partially	in midterm exam.	midterm exam.	
	algorithms satisfying	solution with correct	correct workings			
	CILOs 1 and 2.	workings.				
Final Examination	Able to solve analytical	Excellent if the final	Good if final	Fair if a weak	Marginal if feeble	Not even reaching
	tasks related to	exam has completely	answer is correct	attempt is made	attempt is made in	marginal levels.
	optimization theory and	correct solution with	with partially	for final exam.	final exam.	
	algorithms satisfying	correct workings.	correct workings			
	CILOs 1 and 2.					

#### Part III Other Information (more details can be provided separately in the teaching plan)

## 1. Keyword Syllabus

(An indication of the key topics of the course.)

Convex optimization, Lagrange duality, Linear programming, Quadratic programming, Semidefinite programming, Geometric programming, Parallel and distributed computation methods, First-order and second-order optimization methods, Regularisation, Proximal algorithms, Convex relaxation, Optimization decomposition, Network utility maximization problems, Dynamic programming, Algorithms for combinatorial graph problems, Approximation algorithms in computer science, Algorithms for Internet and wireless networks, Algorithms for machine learning, Algorithms for online social networks, Algorithms for statistical inference and artificial intelligence, Disciplined convex programming and convex optimization software.

### Syllabus

- 1. Overview of optimization theory and algorithms
  - a. Theoretical structures
  - b. Duality approach
  - c. Computational algorithms
- 2. Basic theory: Convex functions and convex sets
- 3. Basic theory: Linear programming and quadratic programming
- 4. Convex optimization theory: conic programming and semidefinite programming
- 5. Convex optimization theory: geometric programming
- 6. Lagrange duality of convex optimization and decomposition
- 7. Primal and dual decomposition and theory of iterative methods
- 8. Disciplined convex programming and convex optimization software
- 9. Application: Algorithms for Internet and wireless network utility maximization
- 10. Proximal algorithms for parallel and distributed computation
- 11. Application: Approximation algorithms in computer science
- 12. Convex relaxation for non-convex optimization
- 13. Application: Regularization-based algorithms in machine learning
- 14. Application: Optimization-based algorithms in artificial intelligence
- 15. Dynamic programming and Bellman's principle of optimality
- 16. Application: Graph algorithms in online social networking and artificial intelligence

### 2. Reading List

## 2.1 Compulsory Readings

(Compulsory readings can include books, book chapters, or journal/magazine articles. There are also collections of e-books, e-journals available from the CityU Library.)

1. Boyd, S. and Vandenberghe. Convex Optimization. Cambridge University Press. Free e-Book online at: <a href="http://www.stanford.edu/~boyd/cvxbook">http://www.stanford.edu/~boyd/cvxbook</a>

#### 2.2 Additional Readings

(Additional references for students to learn to expand their knowledge about the subject.)

1. Bertsekas, D. and Tsitsiklis, J. N. Parallel and Distributed Computation: Numerical Methods. Athena Scientific, 2015.