# **Chapter 1**

# **Overview of Semiconductor Materials and Physics**

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# **Conductivity / Resistivity of Insulators, Semiconductors, and Conductors**



## **Semiconductor Elements**

Period	II	III	IV	V	VI
2		В	С	Ν	
		Boron	Carbon	Nitrogen	
3	Mg	Al	Si	Р	S
	Magnesium	Aluminum	Silicon	Phosphorus	Sulfur
4	Zn	Ga	Ge	As	Se
	Zinc	Gallium	Germanium	Arsenic	Selenium
5	Cd	In	Sn	Sb	Te
	Cadmium	Indium	Tin	Antimony	Tellurium
6	Hg		Pb		
	Mercury		Lead		

# **Element and Compound Semiconductors**

Elements	Compounds	Compounds	Compounds	Compounds
	IV-IV	III-V	II-VI	IV-VI
Si	SiC	AlAs	CdS	PbS
Ge	SiGe	AlSb	CdSe	РbТе
	SiCGe	GaN	CdTe	
		GaAs	ZnS	
		GaP	ZnSe	
		GaSb	ZnTe	
		InAs	ZnO	
		InP		
		InSb		

## **Unit Cells**



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#### **Diamond Lattice**

#### **Zincblende** Lattice



## **Bohr Hydrogen Model**

$$E_{H} = \frac{-m_{o}q^{4}}{8\varepsilon_{o}^{2}h^{2}n^{2}} = \frac{-13.6}{n^{2}}eV$$

 $m_o$  denotes the free electron mass q denotes the electronic charge  $\varepsilon_o$  denotes the free space permittivity h denotes the Plank constant n denotes the principal quantum number

Therefore, for n = 1, that is, ground state,  $E_H = -13.6$  eV

For n = 2, the first excited state,  $E_H = -3.4 \text{ eV}$ 

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Formation of energy bands as a diamond lattice crystal by bringing together isolated silicon atoms







### **Indirect Bandgap**

Inefficient photon emission, requiring change in crystal momentum Direct Bandgap Efficient photon emission



## **Fermi-Dirac Distribution Function**

The probability that an electronic state with energy E is occupied by an electron is given by the Fermi-Dirac distribution function:

$$f(E) = \frac{1}{1 + e^{(E - E_F)/kT}}$$

 $E_F$  is the Fermi level, the energy at which the probability of occupation by an electron is exactly one-half. At room temperature, the intrinsic Fermi level lies very close to the middle of the bandgap.

The effective density of states in the conduction band  $N_C$  is equal to  $2[2\pi m_n kT/h^2]^{3/2}$ . Similarly, the effective density of states in the valence band  $N_V$  is  $2[2\pi m_p kT/h^2]^{3/2}$ . At room temperature,  $N_C$  for silicon is 2.8 x 10<sup>19</sup> atoms/cm<sup>3</sup>.

For an intrinsic semiconductor, the number of electrons per unit volume in the conduction band is equal to the number of holes per unit volume in the valence band. That is,  $n = p = n_i$  where  $n_i$  is the intrinsic carrier density.

- For a doped, or extrinsic, semiconductor, the increase of one type of carriers reduces the number of the other type. Thus, the product of the two types of carriers remains constant at a given temperature
- For Si,  $n_i = 1.45 \times 10^{10} \text{ cm}^{-3}$  and for GaAs,  $n_i = 1.79 \times 10^6 \text{ cm}^{-3}$ . GaAs has a lower intrinsic carrier density on account of its larger bandgap

#### *n-type Si with donor (arsenic)*



The arsenic atom forms covalent bonds with its four neighboring silicon atoms, and the fifth electron becomes a conduction electron, thereby giving rise to a positively charged arsenic atom. The silicon crystal becomes ntype and arsenic is called a donor.

Boron has only three outer shell electrons and is an acceptor in silicon.

*p-type Si with acceptor (boron)* 

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# **Impurities such as arsenic and boron have energy levels very close to the conduction band and valence band, respectively**



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Shallow donors or acceptors exist in ionized form at room temperature because thermal energy is sufficient to ionize them.

This condition is called complete ionization, that is,  $n = N_A$  or  $N_D$ 

Since  $n = N_C \exp\{-(E_C - E_F)/kT\}$ ,  $N_D = N_C \exp\{-(E_C - E_F)/kT\}$  and  $E_C - E_F = kT \ln[N_C/N_D]$ .

 $(E_C - E_F)$  becomes smaller with increasing  $N_D$ , or the Fermi level moves closer to the bottom of the conduction band

For p-type semiconductors, the Fermi level moves towards the top of the valence band with increasing acceptor concentration

- When both donors and acceptors are present simultaneously, the impurity which is present at a higher concentration determines the type of conductivity in the semiconductor
- The electron in an n-type semiconductor is called the majority carrier, whereas the hole in n-type semiconductor is termed the minority carrier
- In a p-type semiconductor, holes are majority carriers and electrons are minority carriers

# **Carrier Mobility**

• Using the theorem of equipartition of energy,  $m_n v_{th}^2/2 = 3kT/2$ , where  $m_n$  is the electron effective mass and  $v_{th}$  is the average thermal velocity

• Electrons in the semiconductor therefore move rapidly in all directions

• The thermal motion of an individual electron can be visualized as a succession of random scattering from collisions with lattice atoms, impurity atoms, and other scattering centers

• The average distance between collisions is called the mean free path, and the average time between collisions is termed the mean free time,  $\tau_c$ 



- When a small electric field,  $\varepsilon$ , is applied to the semiconductor, each electron will experience a force equal to  $-q\varepsilon$  and will be accelerated in opposite direction to the electric field with a drift velocity,  $v_n$ . By Newtonian physics, the momentum of the electron is force times time, that is, equal to  $-q\varepsilon\tau_c$ . Therefore,  $m_nv_n = -q\varepsilon\tau_c$ , or  $v_n = -[q\tau_c/m_n]\varepsilon$
- The drift velocity is proportional to the applied electric field. The proportionality factor is called the electron mobility,  $\mu_n$ , in units of cm<sup>2</sup>/V-s. Hence,  $\nu_n = -\mu_n \varepsilon$  where  $\mu_n = q\tau_c/m_n$
- A similar expression can be written for holes:  $v_p = \mu_p \varepsilon$ . The negative sign is removed here because holes drift in the same direction as the electric field

- Carrier mobility depends on lattice scattering and impurity scattering
- Lattice scattering results from thermal vibrations of the lattice atoms. As lattice vibration is more significant with increasing temperature, mobility decreases. At high temperature, lattice vibration dominates
- Impurity scattering results when a charge carrier travels past an ionized donor or acceptor. The probability of impurity scattering depends on the total impurity concentration. Unlike lattice scattering, impurity scattering becomes less significant at high temperatures because the carriers move faster and are less effectively scattered

### **Electron Mobility Versus Temperature**

Insert shows the theoretical temperature dependence of electron mobility





## **Resistivity and Conductivity**



The electron current density,  $J_n$ , flowing in the sample can be calculated by summing the product of the charge on each electron times the electron's velocity over all electrons per unit volume n

$$J_n = I_n / A = \Sigma(-qv_i) = -qnv_n = qn\mu_n \varepsilon$$



- The total current,  $J = J_n$  (electrons) +  $J_p$  (holes) and  $J = (qn\mu_n + qp\mu_p)\varepsilon$
- The proportionality constant is known as the conductivity,  $\sigma$ . A more commonly used term is the resistivity,  $\rho$ , which is the reciprocal of the conductivity. Thus,  $\rho = \sigma^{-1} = [q(n\mu_n + p\mu_p)]^{-1}$
- Generally, in extrinsic semiconductors, one of the two components is dominant. Therefore, for n-type semiconductors,  $\rho = (qn\mu_n)^{-1}$  and for p-type semiconductors,  $\rho$  $= (qp\mu_p)^{-1}$



### **Resistivity versus impurity concentration**



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## **P-N Junction**



The large carrier concentration gradients at a p-n junction cause carrier diffusion. Holes from the p-side diffuse into the n-side, and electrons from the n-side diffuse into the p-side. This sets up an electric field, which in equilibrium, exactly counteracts these diffusion tendencies and thus permits no net transport of electrons or holes across the junction.

- When a small positive voltage is applied to the p-side, there will be a net movement of holes flowing from the p-side to the n-side, thereby creating a forward bias situation
- If a negative voltage is applied to the pside, i.e. reverse bias condition, the p-n junction becomes an open circuit. A p-n junction therefore acts as a diode

## **Recombination Processes**

- When the thermal equilibrium in a semiconductor is perturbed, that is, the product, **np**, is no longer equal to  $n_i^2$ , by injection of excess carriers, processes exist to restore the system back to equilibrium  $(np = n_i^2)$
- If the released energy results in the emission of a photon, the process is called radiative recombination, otherwise it is called nonradiative recombination
- When excess carriers are introduced to a direct-bandgap semiconductor such as GaAs, the probability is high that electrons and holes will recombine directly and a photon is emitted



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### **Light-Emitting Diodes**

Light emitting diodes (LEDs) are p-n junctions that emit spontaneous radiation in ultraviolet, visible, or infrared region under bias. The most common visible LEDs are made of alloys of  $GaAs_{1-y}P_y$ , where y is the atomic fraction. The bandgap of the alloy depends on its composition, i.e. y, thus implying that the emitted light frequency can be tailored by altering y.

### **Semiconductors of interest as visible LEDs**





# Metal-Oxide Semiconductor Field Effect Transistor (MOSFET)



### **Enhancement Mode**

**Depletion Mode** 





**Complementary MOS** (CMOS)

- low current

- low power consumption



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